

BLAS Fortran 77 prototypes

Level 1 blas: vector, $O(n)$ operations

name (dim, scalar, vector, vector, scalars, param)	description	equation	prefixes
_rotg (a, b, c, s)	generate plane rotation		s, d
_rotmg (d1, d2, a, b, param)	generate modified plane rotation		s, d
_rot (n, x, incx, y, incy, c, s)	apply plane rotation		s, d
_rotm (n, x, incx, y, incy, param)	apply modified plane rotation		s, d
_swap (n, x, incx, y, incy)	swap vectors	$x \leftrightarrow y$	s, d, c, z
_scal (n, alpha, x, incx)	scale vector	$y = \alpha y$	s, d, c, z, cs, zd
_copy (n, x, incx, y, incy)	copy vector	$y = x$	s, d, c, z
_axpy (n, alpha, x, incx, y, incy)	update vector	$y = y + \alpha x$	s, d, c, z
_dot (n, x, incx, y, incy)	dot product	$= x^t y$	s, d, ds
_dotu (n, x, incx, y, incy)	(complex)	$= x^t y$	c, z
_dotc (n, x, incx, y, incy)	(complex conj)	$= x^h y$	c, z
_ddot (n, x, incx, y, incy)	(?)	$= \alpha + x^t y$	sds
_nrm2 (n, x, incx)	2-norm	$= \ x\ _2$	s, d, sc, dz
_asum (n, x, incx)	1-norm	$= \ \operatorname{Re}(x)\ _1 + \ \operatorname{Im}(x)\ _1$	s, d, sc, dz
i_amax (n, x, incx)	∞ -norm	$= i$ such that $ \operatorname{Re}(x_i) + \operatorname{Im}(x_i) $ is max	s, d, c, z

Level 2 blas: matrix-vector, $O(n^2)$ operations

name (options, dim, bandwidth, scalar, matrix, vector, scalar, vector)	description	equation	prefixes
_gemv (trans, m, n, alpha, A, ldA, x, incx, beta, y, incy)	general matrix-vector multiply	$y = \alpha A^* x + \beta y$	s, d, c, z
_gbmv (trans, m, n, kl, ku, alpha, A, ldA, x, incx, beta, y, incy)	(banded)	$y = \alpha A^* x + \beta y$	s, d, c, z
_hemv (uplo, n, alpha, A, ldA, x, incx, beta, y, incy)	hermetian mat-vec	$y = \alpha Ax + \beta y$	c, z
_hbm (uplo, n, k, alpha, A, ldA, x, incx, beta, y, incy)	(banded)	$y = \alpha Ax + \beta y$	c, z
_hpmv (uplo, n, alpha, Ap, x, incx, beta, y, incy)	(packed)	$y = \alpha Ax + \beta y$	c, z
_symv (uplo, n, alpha, A, ldA, x, incx, beta, y, incy)	symmetric mat-vec	$y = \alpha Ax + \beta y$	s, d, (c, z)†
_sbmv (uplo, n, k, alpha, A, ldA, x, incx, beta, y, incy)	(banded)	$y = \alpha Ax + \beta y$	s, d
_spmv (uplo, n, alpha, Ap, x, incx, beta, y, incy)	(packed)	$y = \alpha Ax + \beta y$	s, d, (c, z)†
_trmv (uplo, trans, diag, n, A, ldA, x, incx)	triangular mat-vec	$x = A^* x$	s, d, c, z
_tbmv (uplo, trans, diag, n, k, A, ldA, x, incx)	(banded)	$x = A^* x$	s, d, c, z
_tpmv (uplo, trans, diag, n, Ap, x, incx)	(packed)	$x = A^* x$	s, d, c, z
_trsv (uplo, trans, diag, n, A, ldA, x, incx)	triangular solve	$x = A^{-*} x$	s, d, c, z
_tbsv (uplo, trans, diag, n, k, A, ldA, x, incx)	(banded)	$x = A^{-*} x$	s, d, c, z
_tpsv (uplo, trans, diag, n, Ap, x, incx)	(packed)	$x = A^{-*} x$	s, d, c, z

A^* denotes A, A^T , or A^H ;

A^{-*} denotes A^{-1}, A^{-T} , or A^{-H} , depending on options and data type.

A is $m \times n$ or $n \times n$.

Level 2, continued

name (options, dim, scalar, vector, vector, matrix)	description	equation	prefixes
_ger (m, n, alpha, x, incx, y, incy, A, ldA)	general rank-1 update	$A = A + \alpha xy^T$	s, d
_geru (m, n, alpha, x, incx, y, incy, A, ldA)	(complex)	$A = A + \alpha xy^T$	c, z
_gerc (m, n, alpha, x, incx, y, incy, A, ldA)	(complex conj)	$A = A + \alpha xy^H$	c, z
_her (uplo, n, alpha, x, incx, A, ldA)	hermetian rank-1 update	$A = A + \alpha xx^H$	c, z
_hpr (uplo, n, alpha, x, incx, Ap)	(packed)	$A = A + \alpha xx^H$	c, z
_her2 (uplo, n, alpha, x, incx, y, incy, A, ldA)	hermetian rank-2 update	$A = A + \alpha xy^H + y(\alpha x)^H$	c, z
_hpr2 (uplo, n, alpha, x, incx, y, incy, Ap)	(packed)	$A = A + \alpha xy^H + y(\alpha x)^H$	c, z
_syr (uplo, n, alpha, x, incx, A, ldA)	symmetric rank-1 update	$A = A + \alpha xx^T$	s, d, (c, z)†
_spr (uplo, n, alpha, x, incx, Ap)	(packed)	$A = A + \alpha xx^T$	s, d, (c, z)†
_syr2 (uplo, n, alpha, x, incx, y, incy, A, ldA)	symmetric rank-2 update	$A = A + \alpha xy^T + \alpha yx^T$	s, d
_spr2 (uplo, n, alpha, x, incx, y, incy, Ap)	(packed)	$A = A + \alpha xy^T + \alpha yx^T$	s, d

Level 3 blas: matrix-matrix, $O(n^3)$ operations

name (options, dim, scalar, matrix, matrix, scalar, matrix)	description	equation	prefixes
_gemm (transa, transb, m, n, k, alpha, A, ldA, B, ldB, beta, C, ldC)	general matrix-matrix multiply	$C = \alpha A^* B^* + \beta C$	s, d, c, z
_symm (side, uplo, m, n, alpha, A, ldA, B, ldB, beta, C, ldC)	symmetric mat-mat	$C = \alpha AB + \beta C$	s, d, c, z
_hemm (side, uplo, m, n, alpha, A, ldA, B, ldB, beta, C, ldC)	hermetian mat-mat	$C = \alpha AB + \beta C$	c, z
_syrk (uplo, trans, n, k, alpha, A, ldA, beta, C, ldC)	symmetric rank- k update	$C = \alpha AA^T + \beta C$	s, d, c, z
_herk (uplo, trans, n, k, alpha, A, ldA, beta, C, ldC)	hermetian rank- k update	$C = \alpha AA^H + \beta C$	c, z
_syr2k (uplo, trans, n, k, alpha, A, ldA, B, ldB, beta, C, ldC)	symmetric rank- $2k$ update	$C = \alpha AB^T + \bar{\alpha} BA^T + \beta C$	s, d, c, z
_her2k (uplo, trans, n, k, alpha, A, ldA, B, ldB, beta, C, ldC)	hermetian rank- $2k$ update	$C = \alpha AB^H + \bar{\alpha} BA^H + \beta C$	c, z
_trmm (side, uplo, transa, diag, m, n, alpha, A, ldA, B, ldB)	triangular mat-mat	$B = \alpha A^* B$ or $B = \alpha BA^*$	s, d, c, z
_trsm (side, uplo, transa, diag, m, n, alpha, A, ldA, B, ldB)	triangular solve mat	$B = \alpha A^{-*} B$ or $B = \alpha BA^{-*}$	s, d, c, z

A^* denotes A , A^T , or A^H ;

A^{-*} denotes A^{-1} , A^{-T} , or A^{-H} , depending on options and data type.

The destination matrix is $m \times n$ or $n \times n$. For mat-mat, the common dimension of A and B is k .

Prefixes

s – real (float) d – double
c – complex z – complex*16
ge – general gb – general banded
sy – symmetric sb – symmetric banded sp – symmetric packed
he – hermetian hb – hermetian banded hp – hermetian packed
tr – triangular tb – triangular banded tp – triangular packed

† LAPACK adds these complex symmetric routines.

Options

trans = 'N' o transpose: A , 'T'ranspose: A^T , 'C'onjugate transpose: A^H
uplo = 'U' pper triangular, 'L'ower triangular
diag = 'N' on-unit triangular, 'U' nit triangular
side = 'L' eft: AB , 'R' ight: BA
ldA is major stride—number of rows of parent matrix A . Useful for submatrices.

For real matrices, transx = 'T' and 'C' are the same.

For Hermitian matrices, transx = 'T' is not allowed.

For complex symmetric matrices, transx = 'C' is not allowed.

Updated June 13, 2008. BLAS and LAPACK guides available from <http://www.ews.uiuc.edu/~mrgates2/>.

Reference: *BLAS Quick Reference Guide* from <http://www.netlib.org/blas/faq.html>

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